

Space

An Alternate Elective after Algebra II



Henri Picciotto

MathEducation.page

Space: topics

◇ Transformational geometry

- Abstract algebra

◇ Symmetry

- Tiling

◇ Dimension

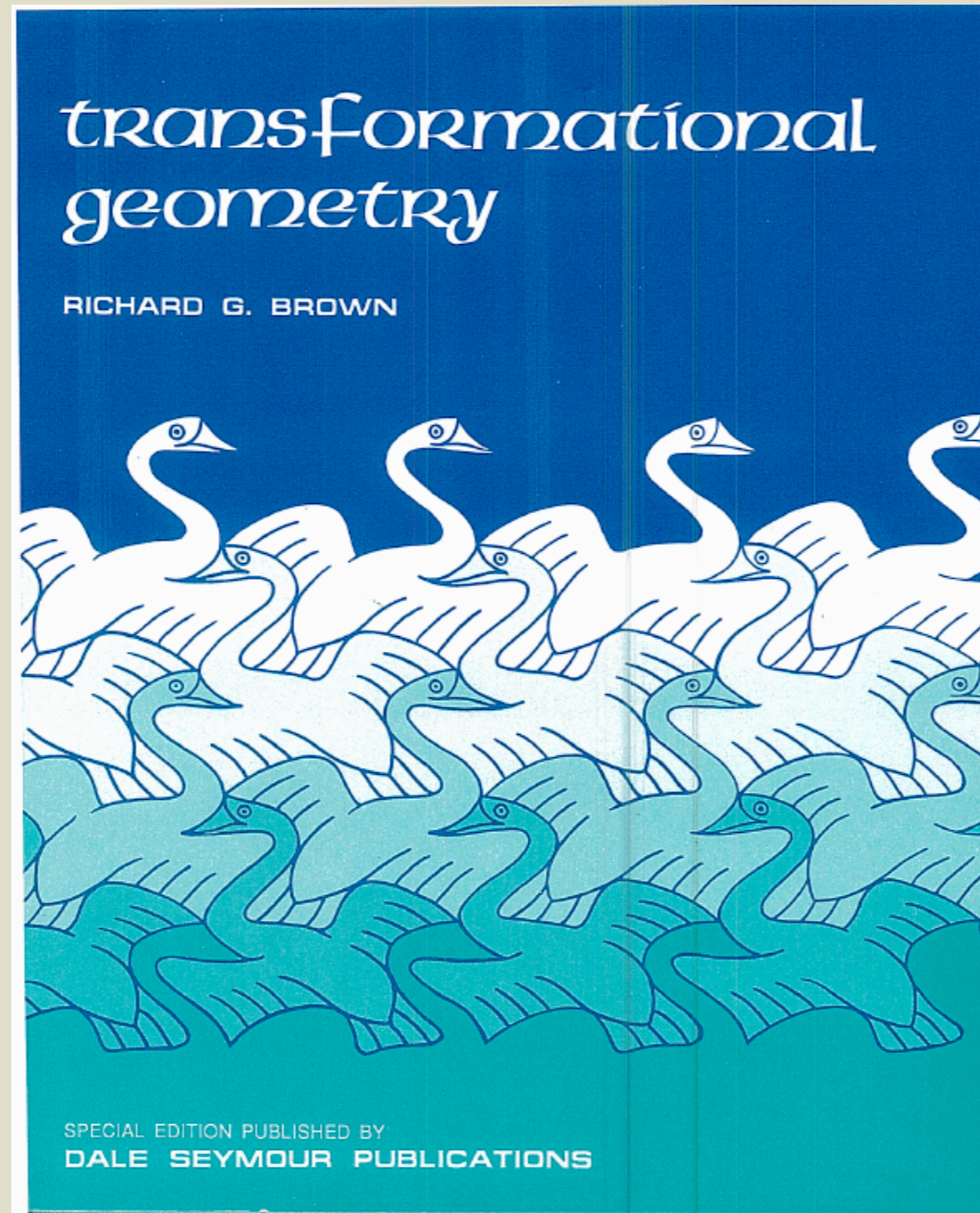
- 3D: polyhedra

- 4D: introduction

Transformations

Symmetry

Dimension



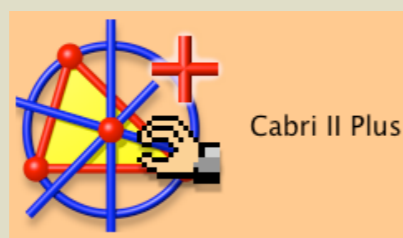
Fundamental Theorem of Isometries:
every isometry of the plane is a reflection, a rotation, a translation, or a glide reflection.

Computing transformations using complex numbers:

◇ Translation: add $a+bi$

◇ Rotation around the origin:
multiply by $\cos \theta + i \sin \theta$

◇ Rotation around (a,b) : subtract $a+bi$,
rotate around the origin, add $a+bi$



Transformations

Symmetry

Dimension

Computing transformations using matrices



Space: topics

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◇ **Symmetry**

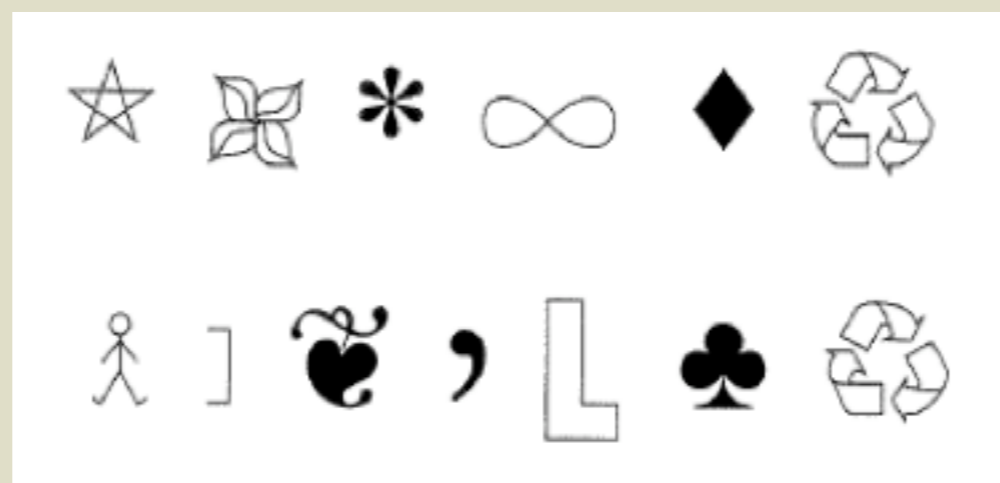
- Tiling

◇ Dimension

- 3D: polyhedra

- 4D: introduction

Transformations
Symmetry
Dimension



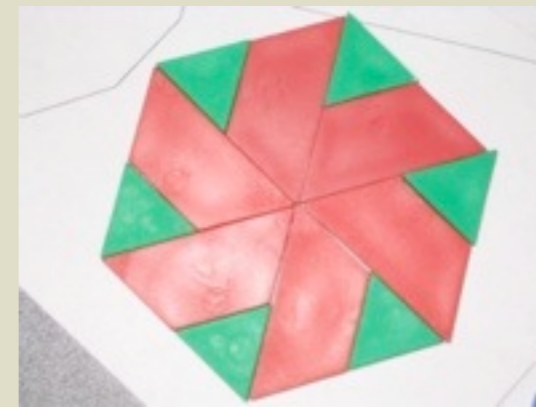
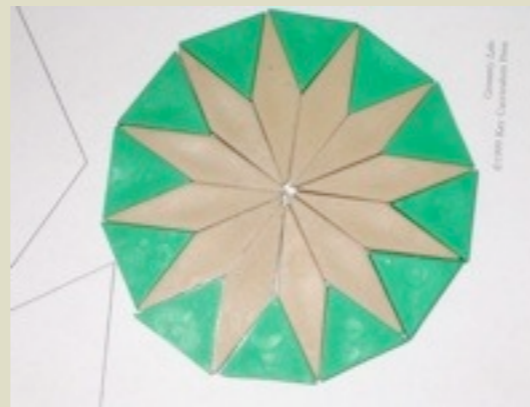
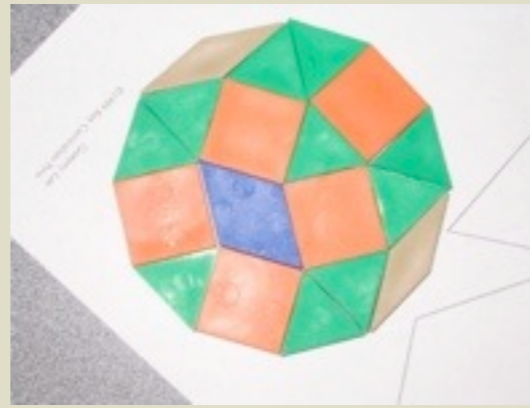
Transformations
Symmetry
Dimension



Transformations

Symmetry

Dimension



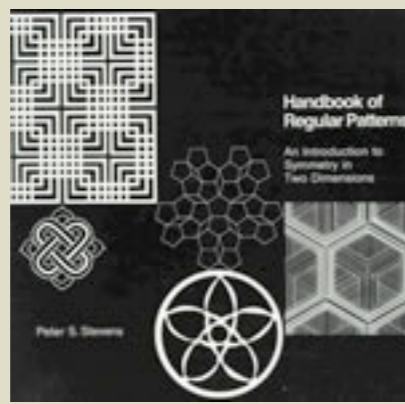
Transformations
Symmetry
Dimension

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Handbook of Regular Patterns by Peter Stevens

The Seven Line Symmetry Groups



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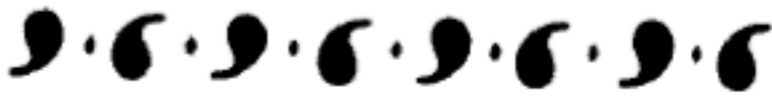
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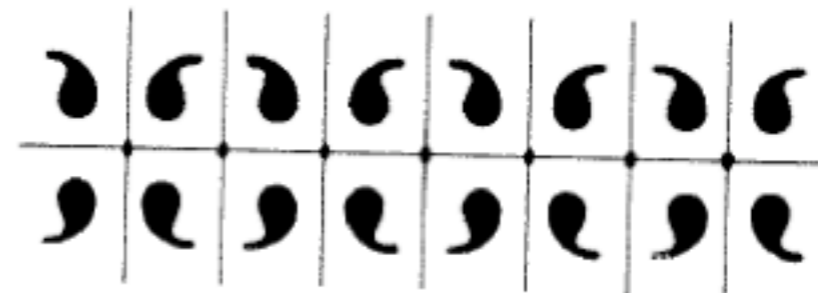
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T2



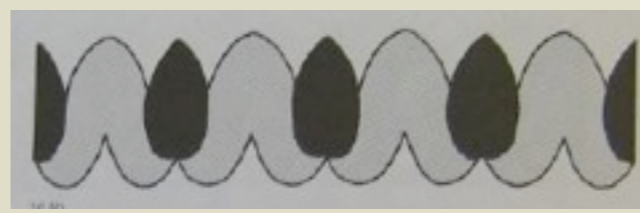
T2MG



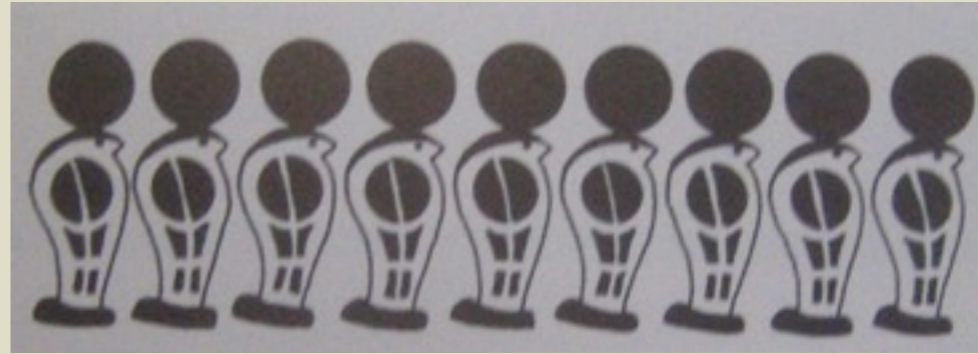
T2MM

Transformations
Symmetry
Dimension

a.



b.



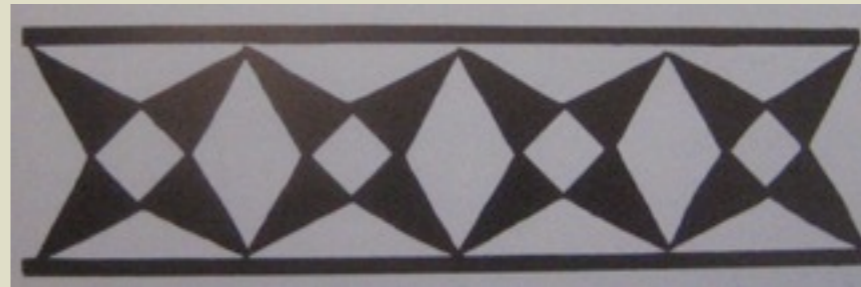
c.



d.



e.



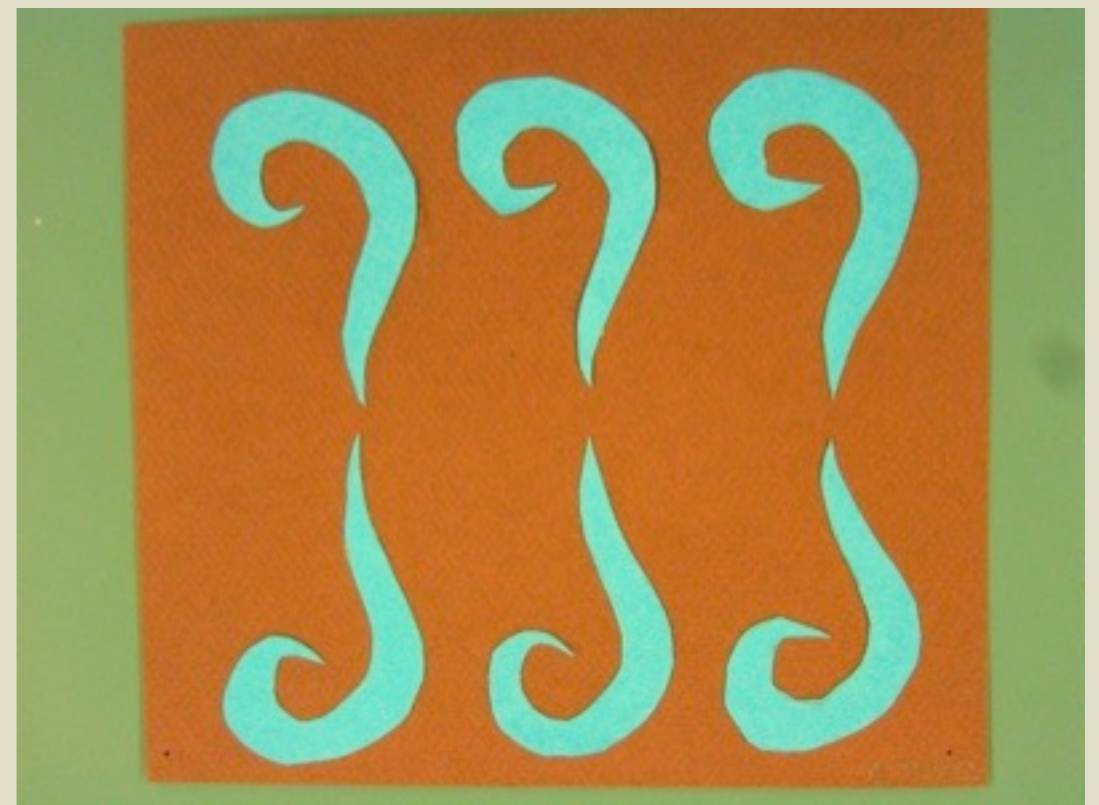
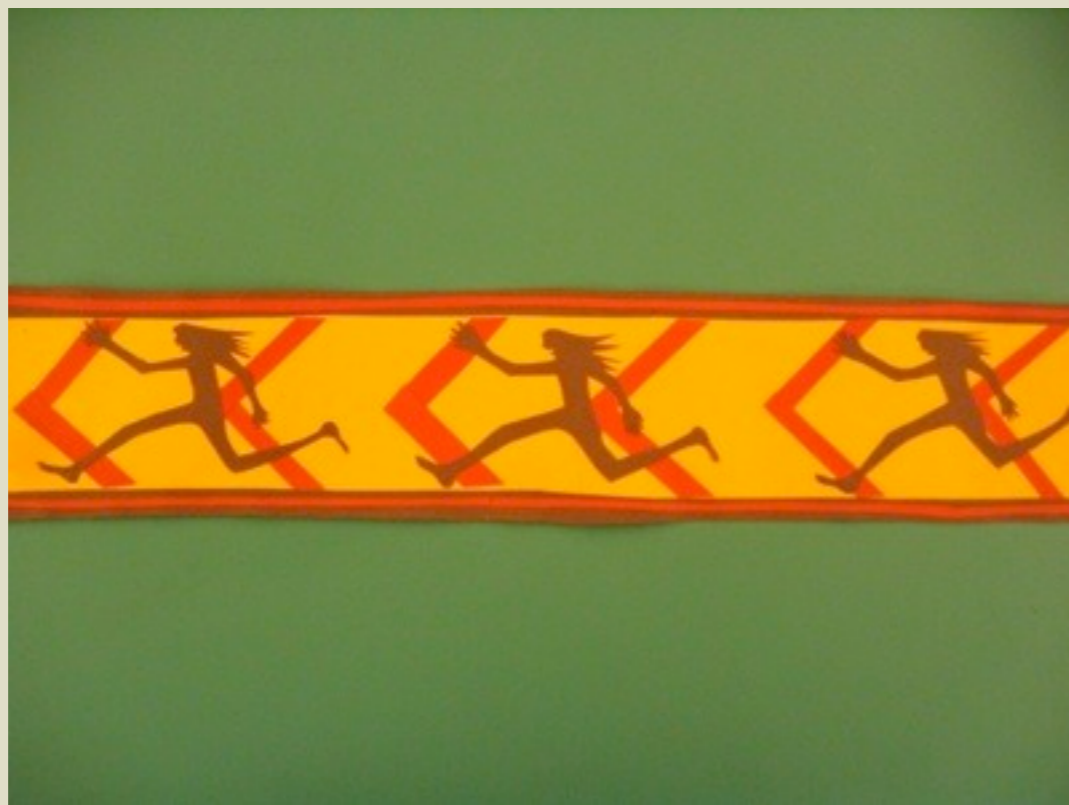
f.



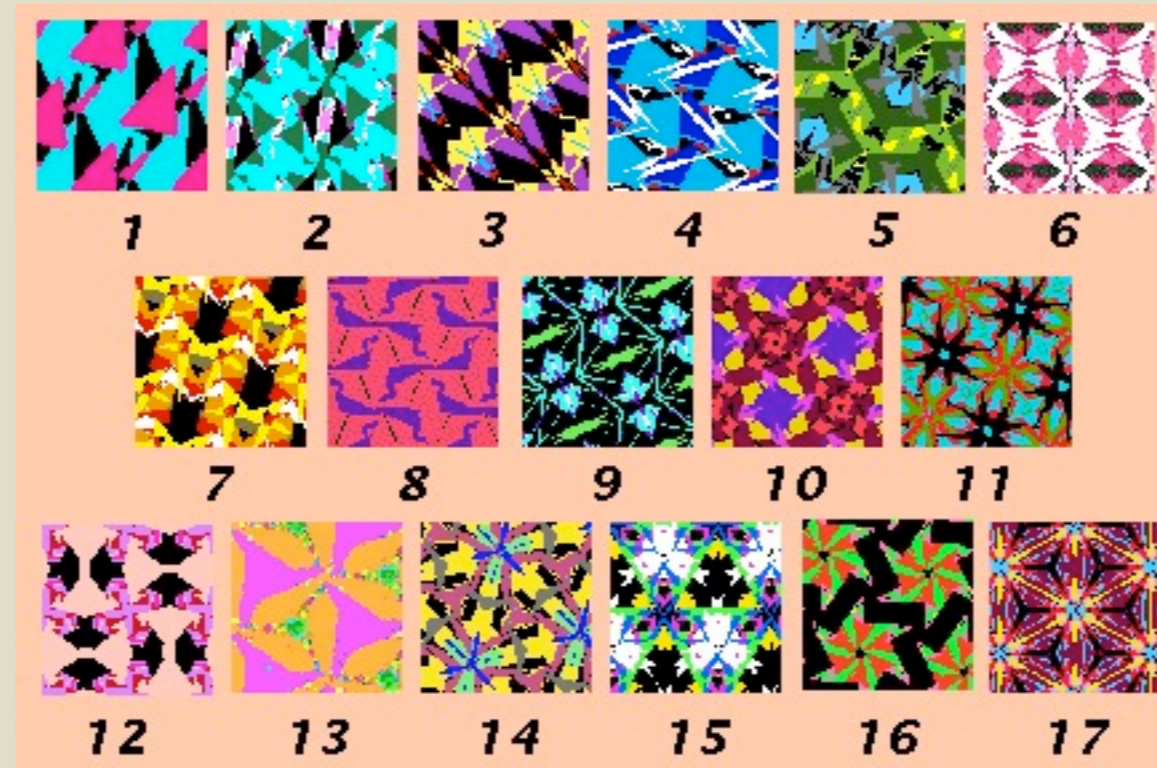
g.



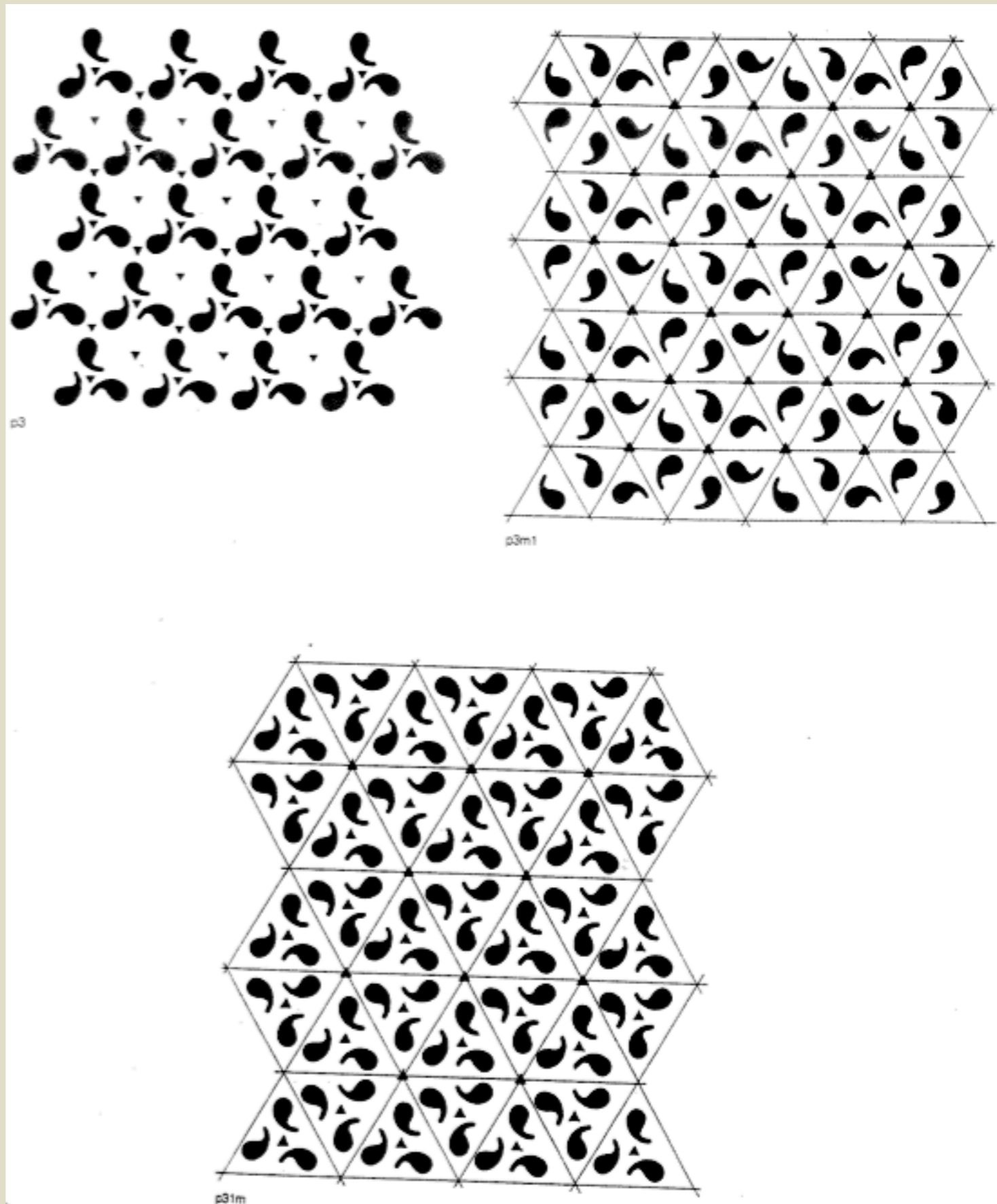
Transformations
Symmetry
Dimension



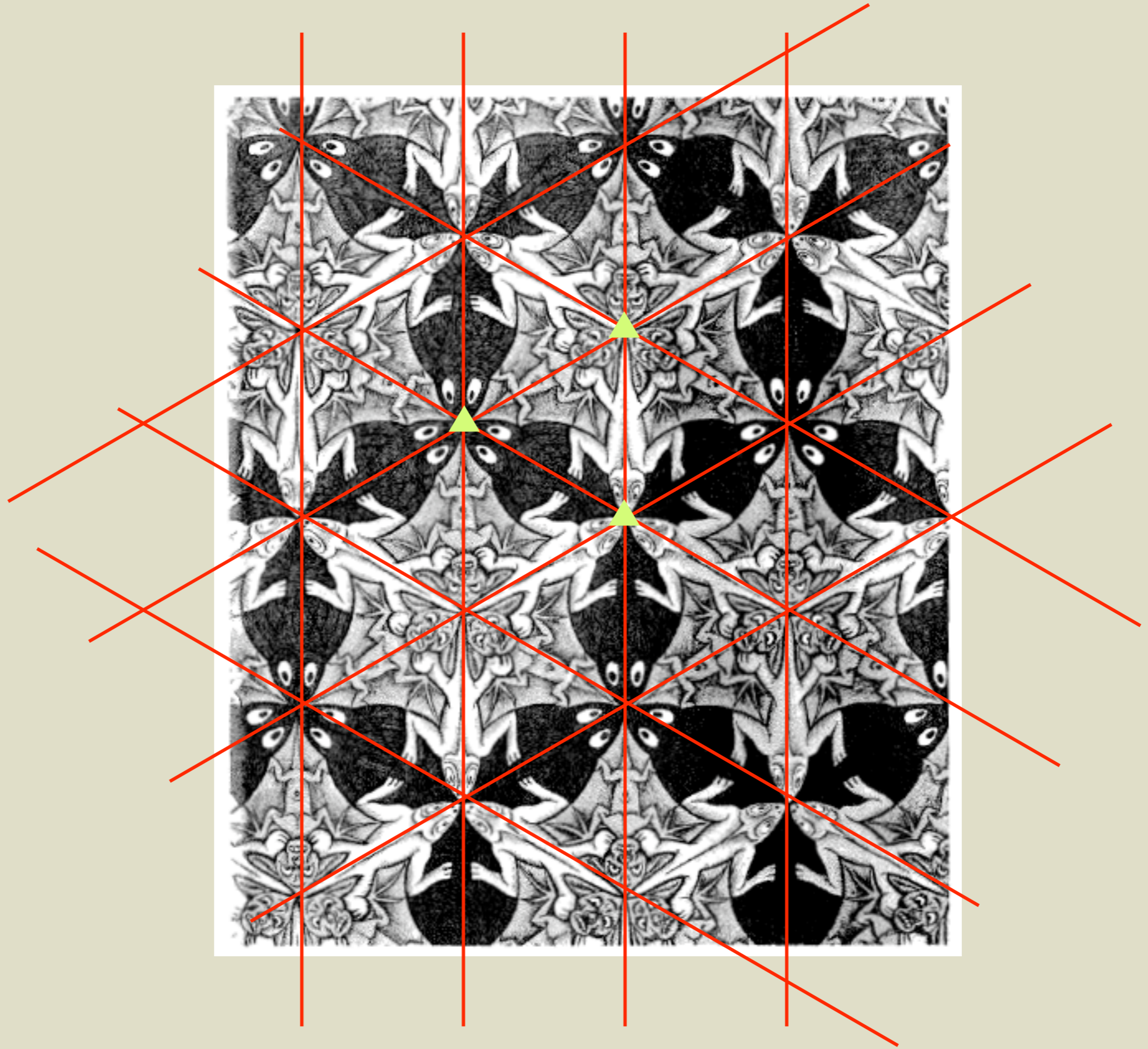
Transformations
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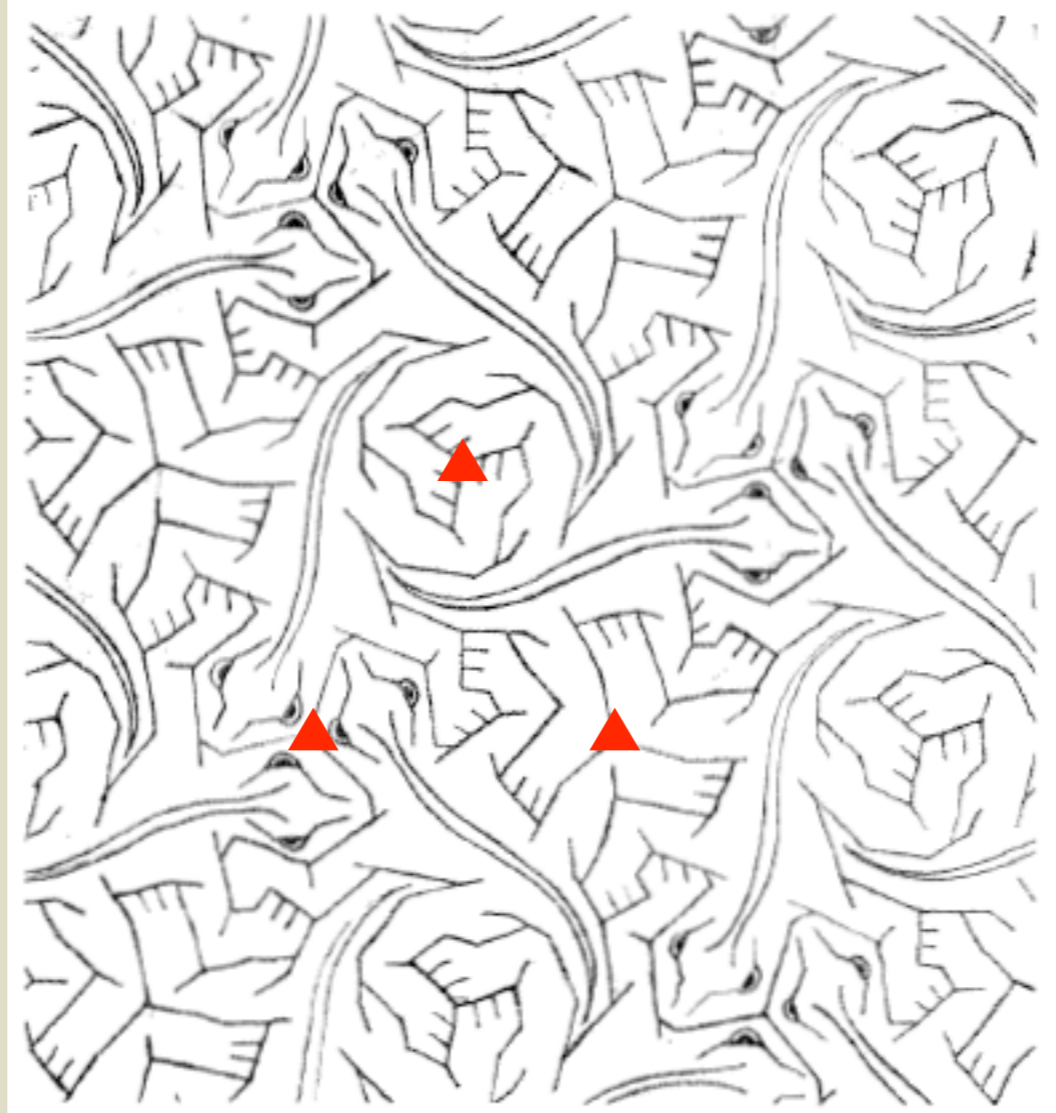
Transformations
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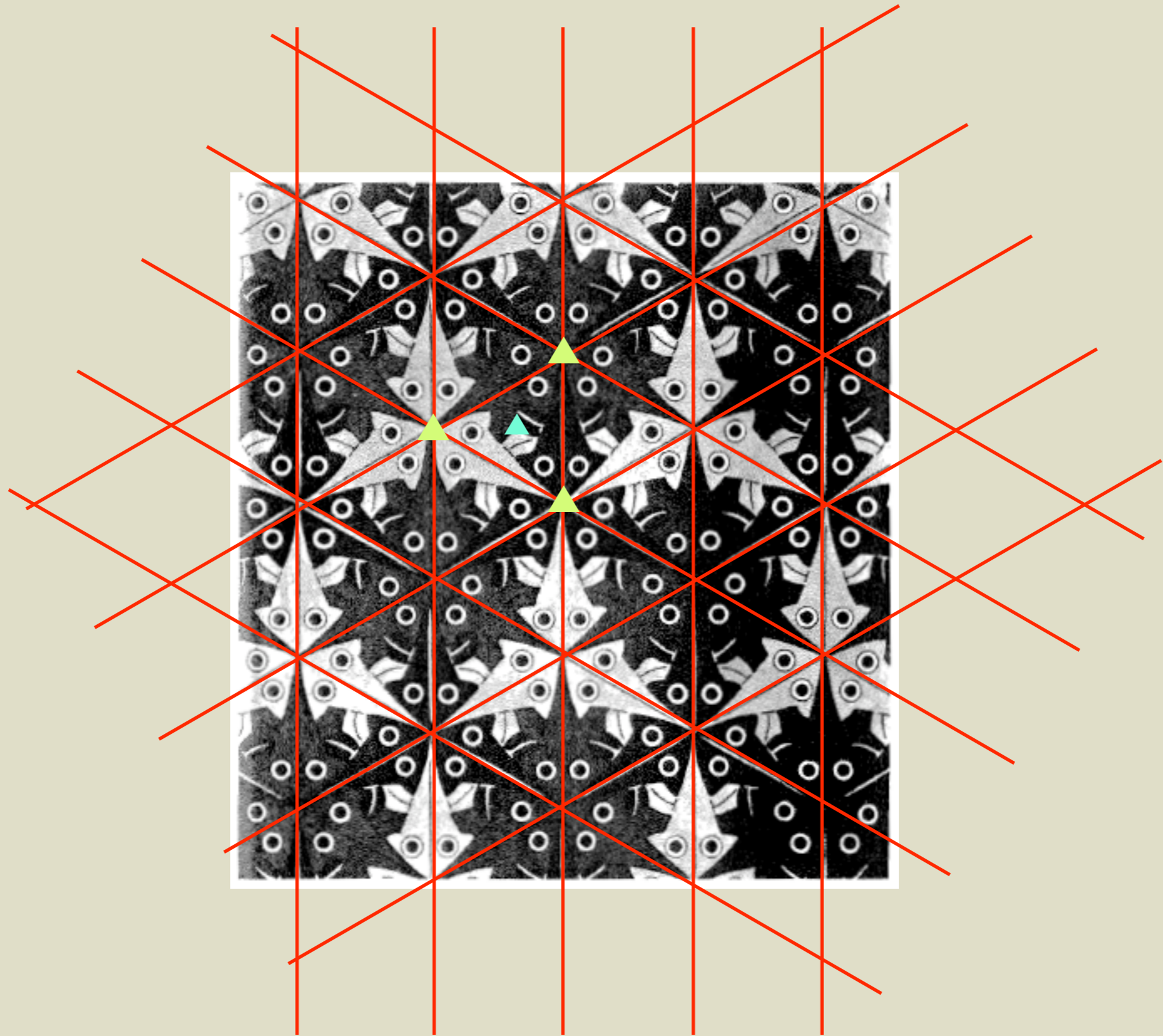
Transformations
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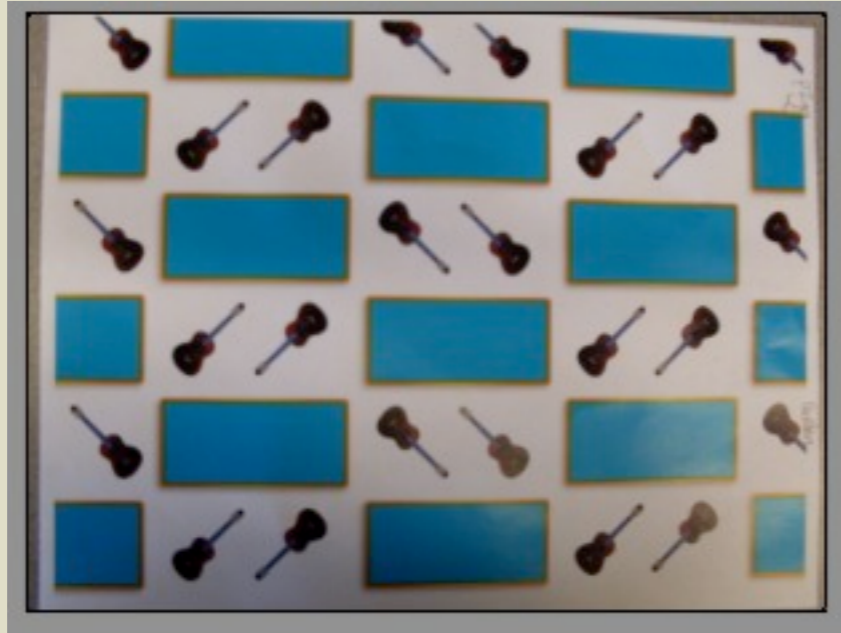
Transformations
Symmetry
Dimension



Transformations
Symmetry
Dimension



Transformations
Symmetry
Dimension



Space: topics

◇ Transformational geometry

- Abstract algebra

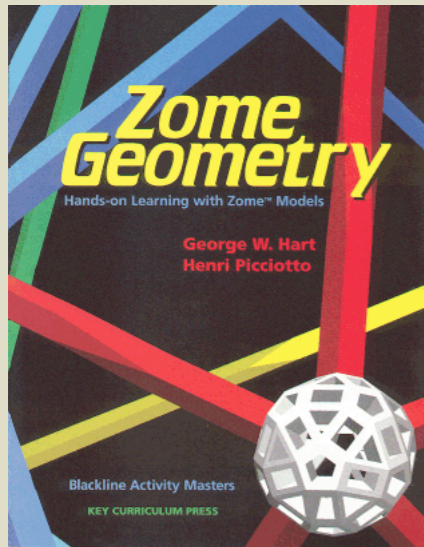
◇ Symmetry

- Tiling

◇ **Dimension**

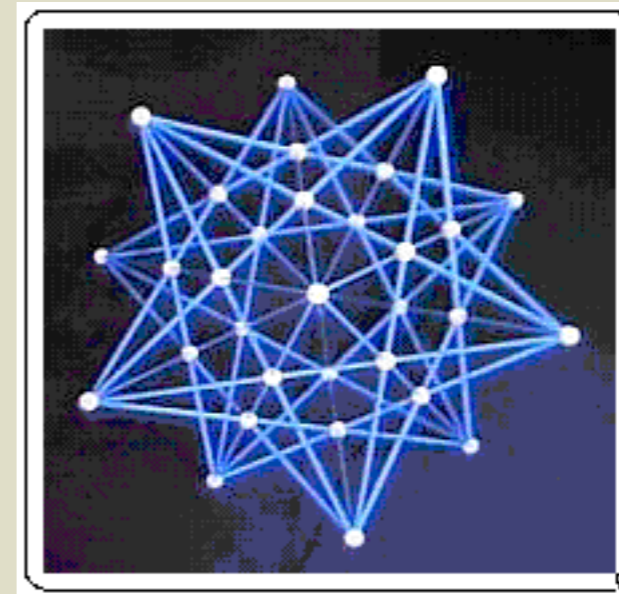
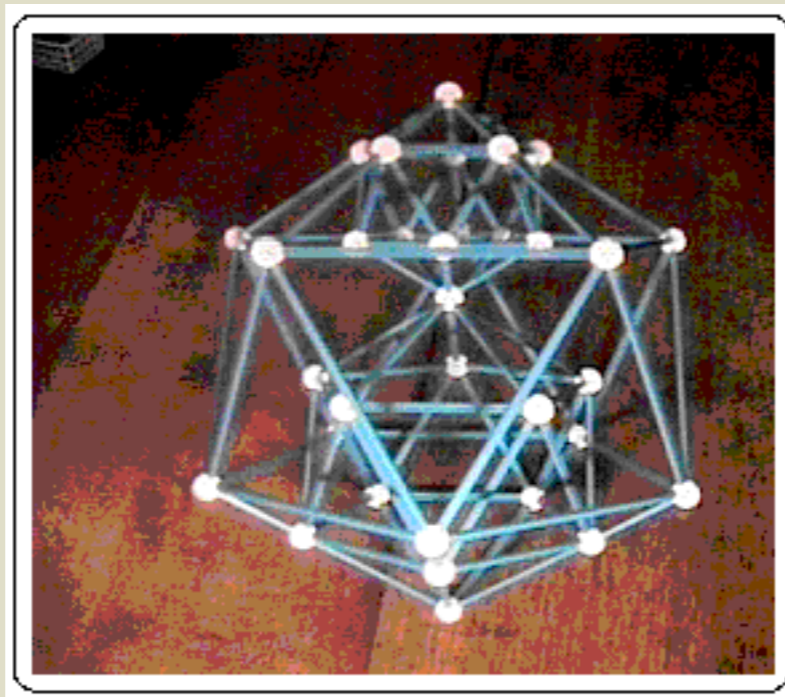
- 3D: polyhedra

- 4D: introduction

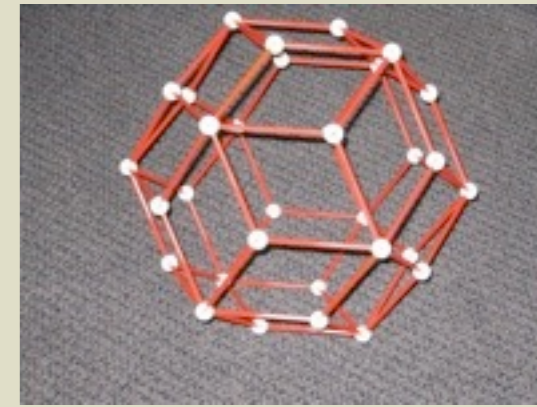
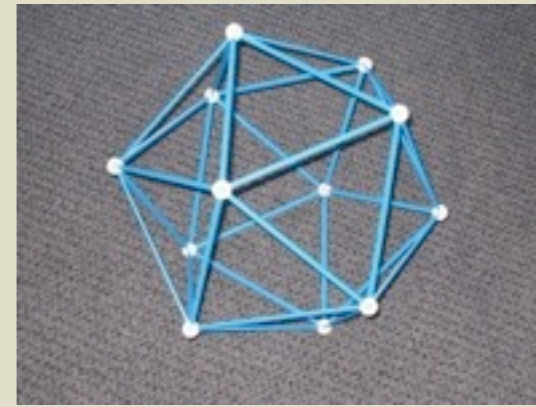
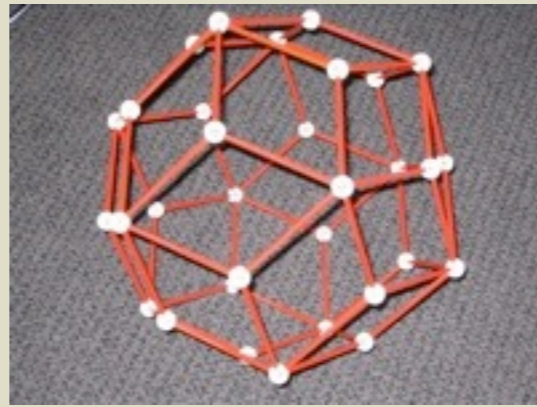
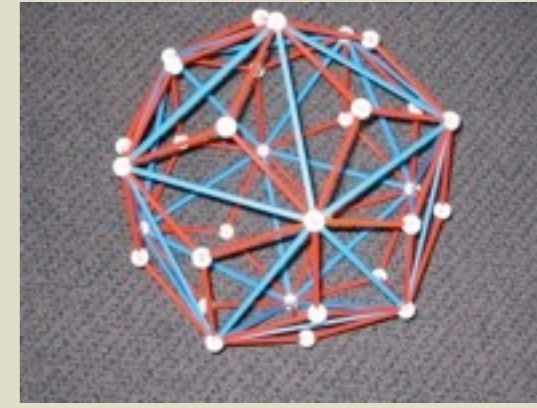
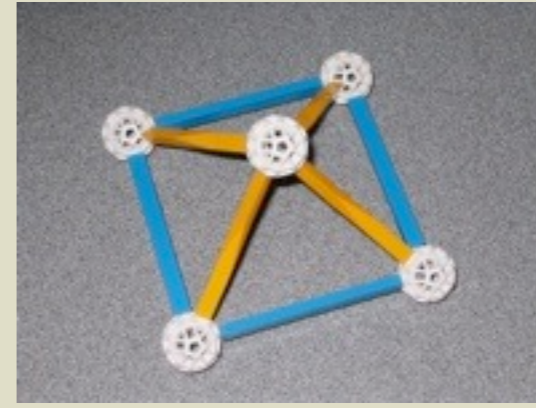
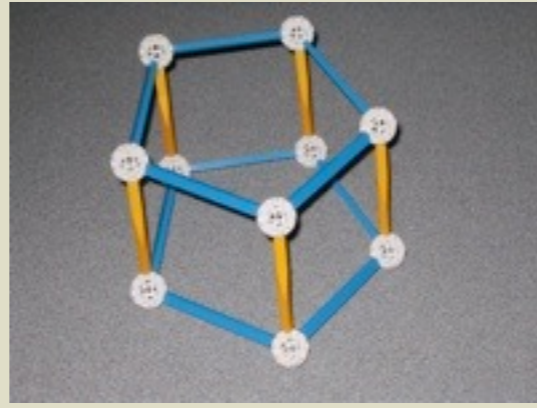
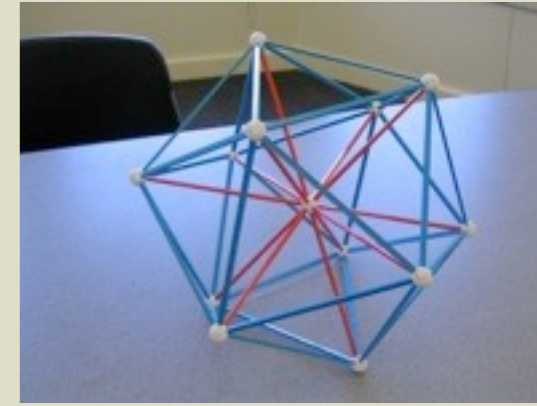
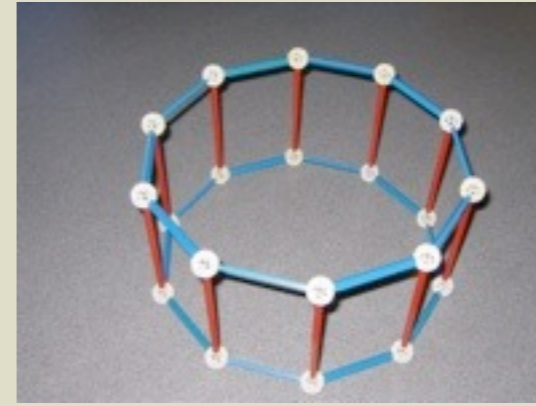
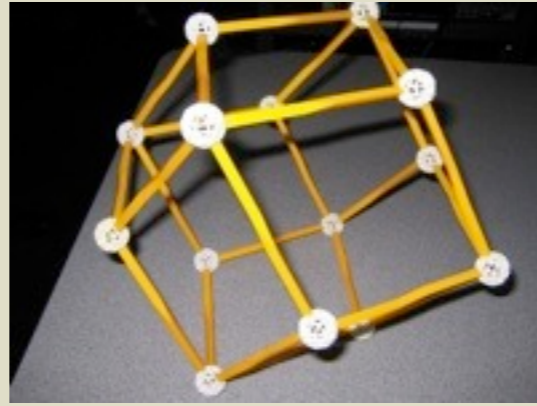
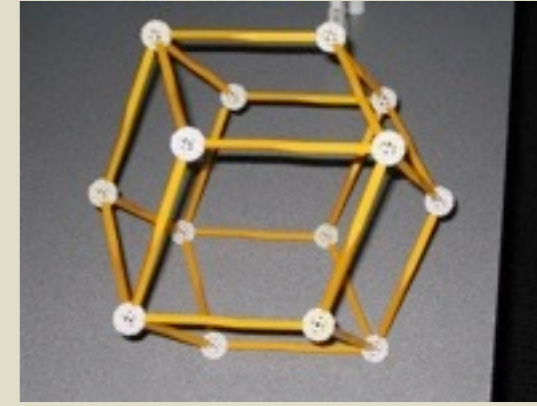
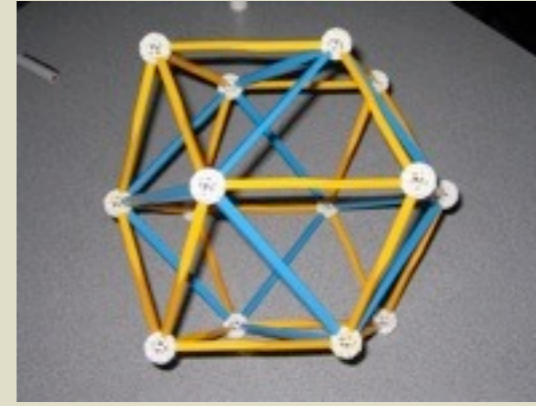
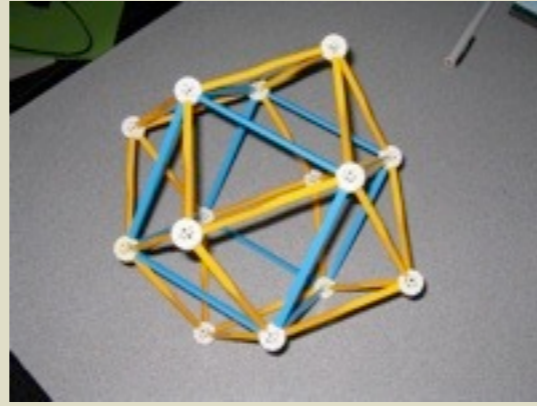
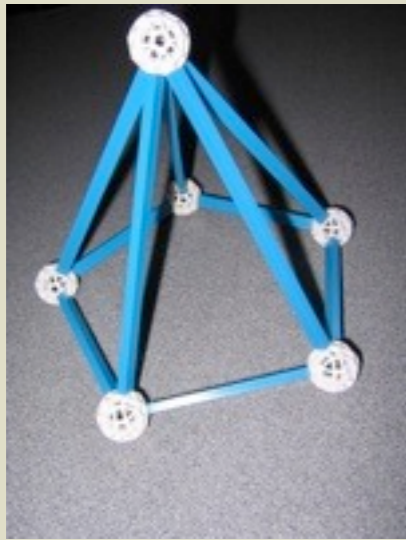


- ◇ Platonic and Archimedean polyhedra
- ◇ Duality
- ◇ Euler's and Descartes' theorems
- ◇ Review of geometry and trigonometry

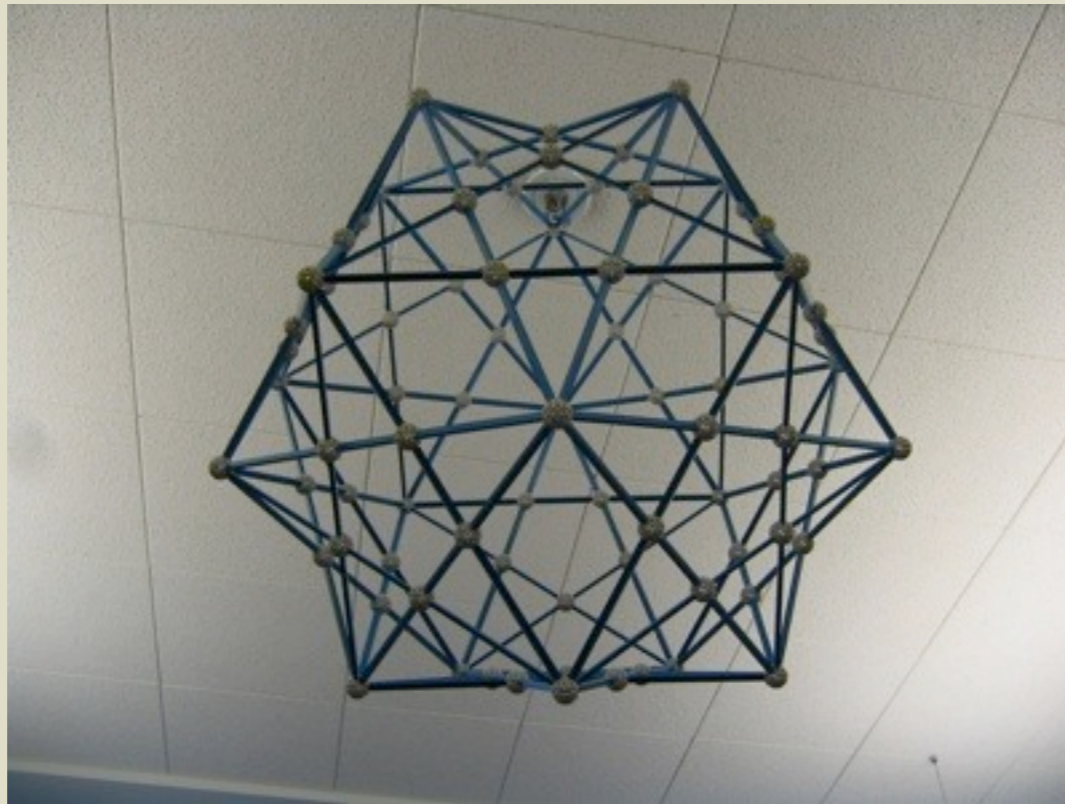
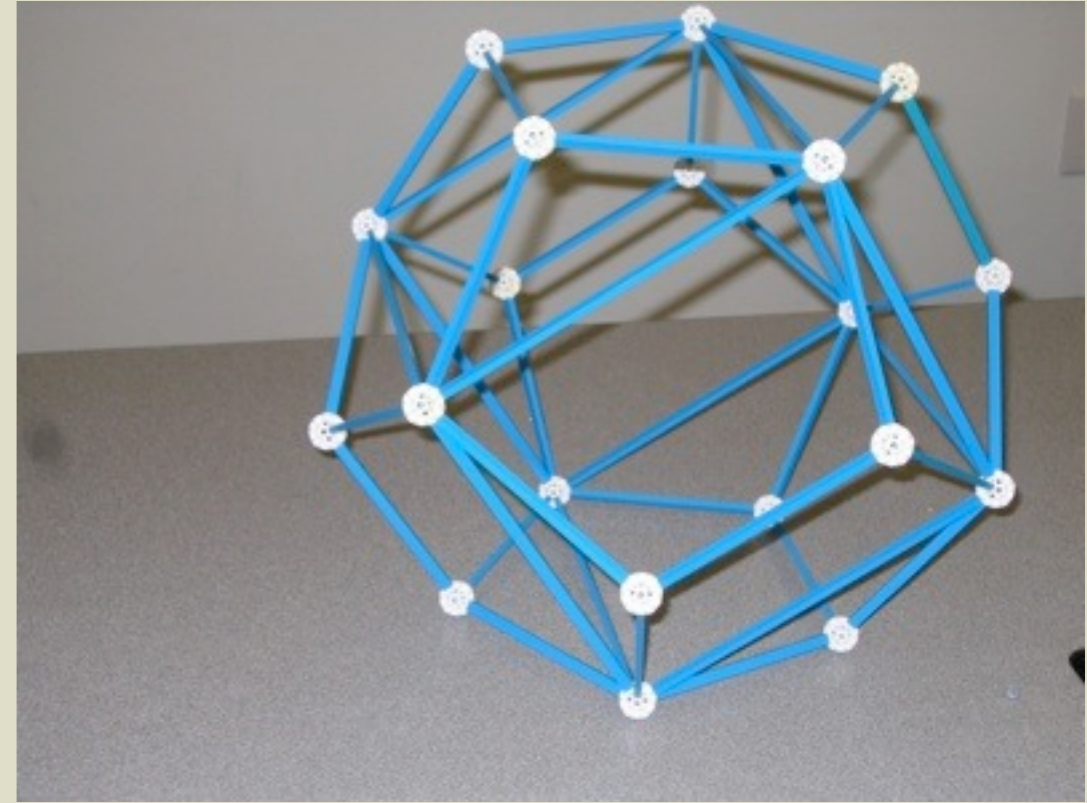
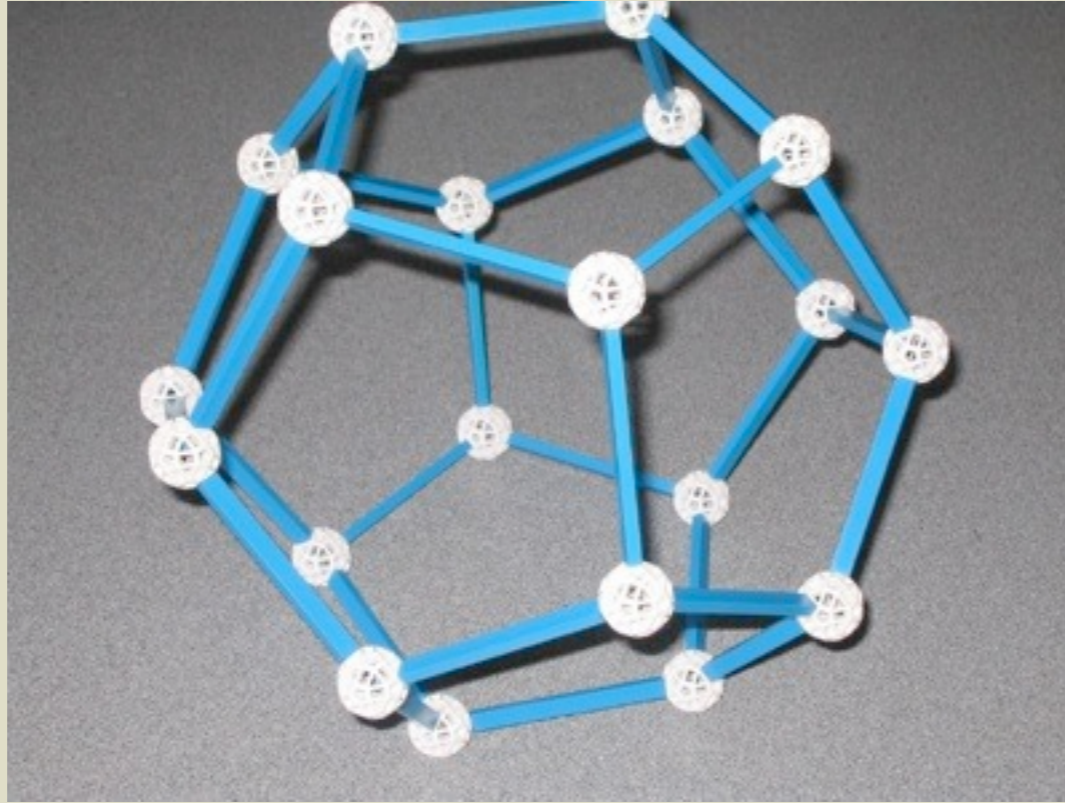
The chief reason for studying regular polyhedra is still the same as in the time of the Pythagoreans, namely, that their symmetrical shapes appeal to one's artistic sense.
---H.S.M. Coxeter



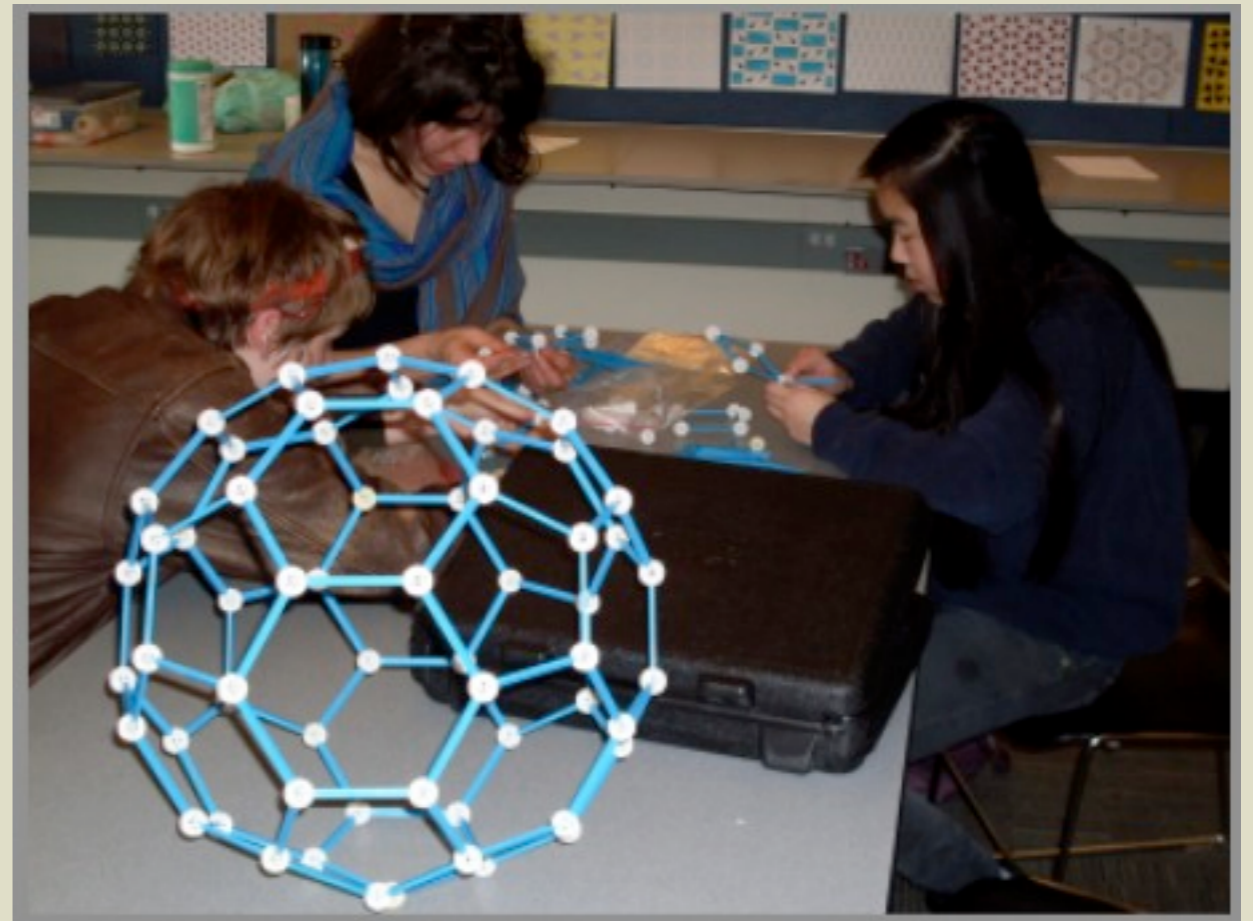
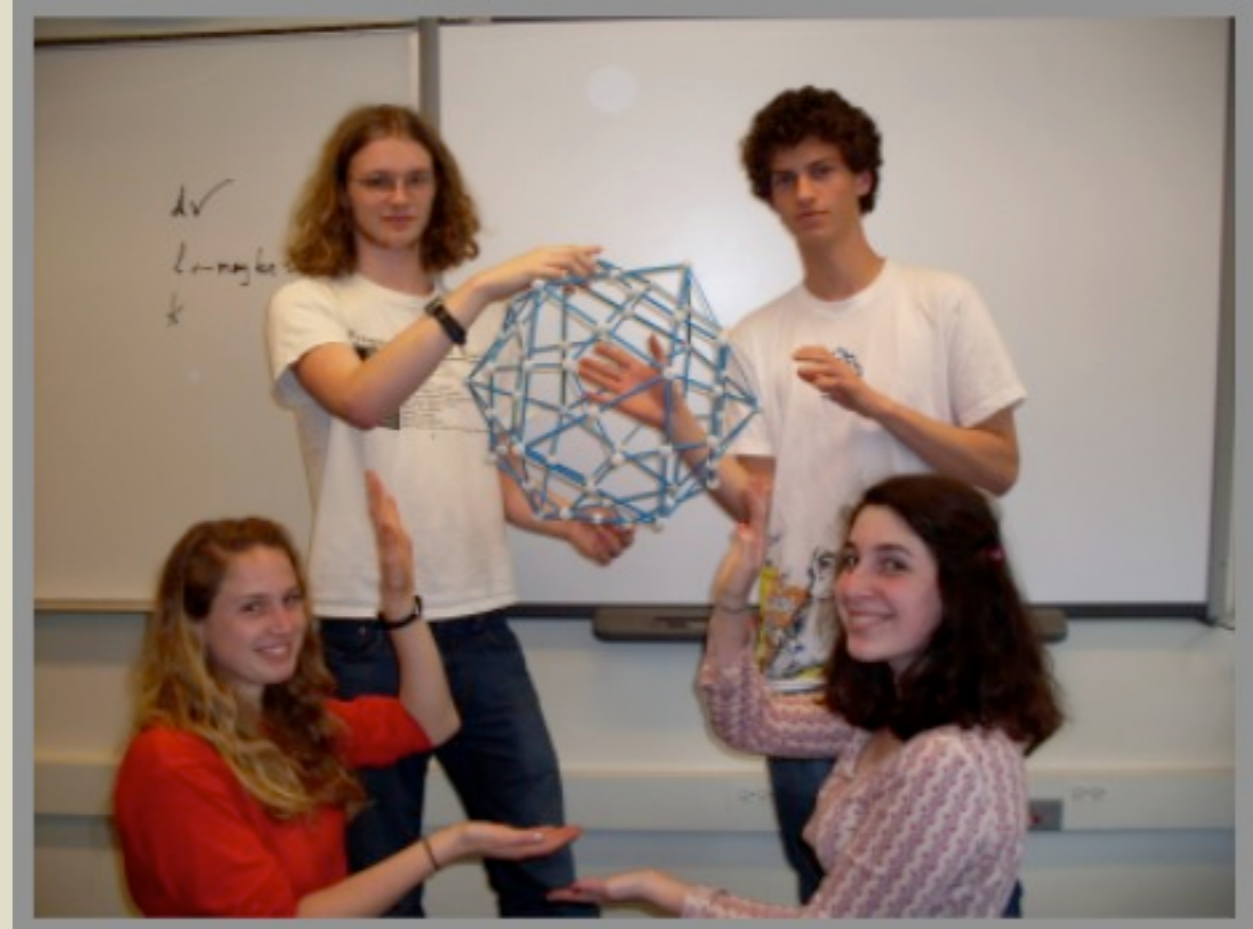
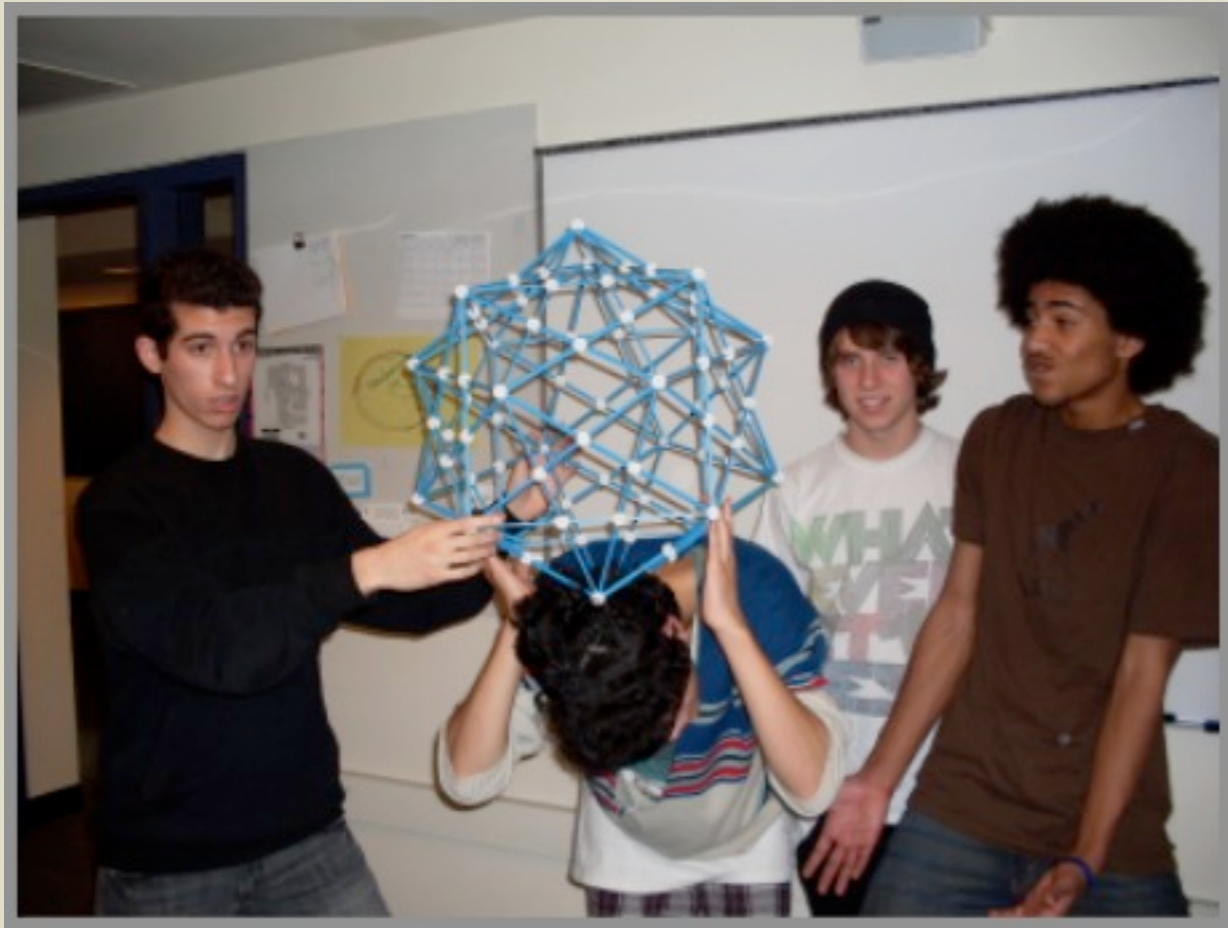
Transformations
Symmetry
Dimension: 3D



Transformations
Symmetry
Dimension: 3D



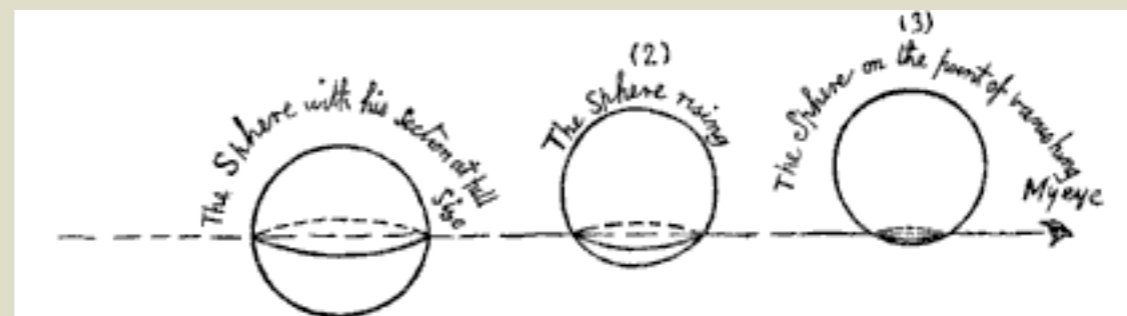
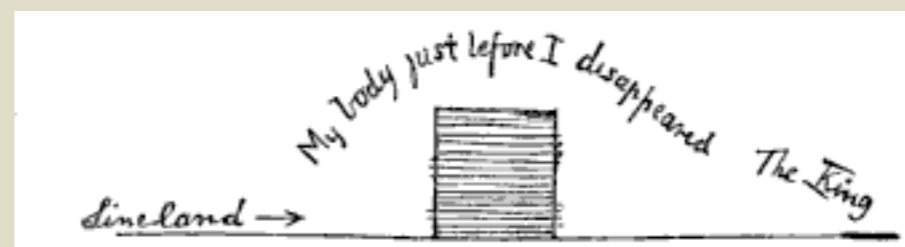
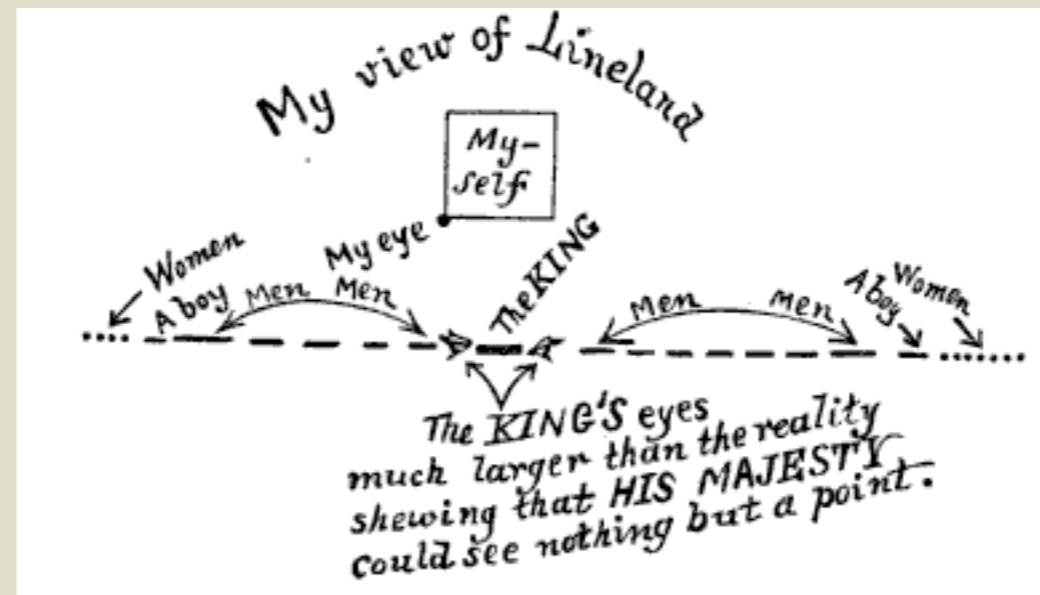
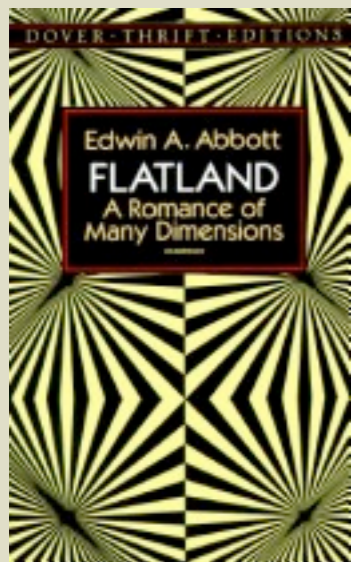
Transformations
Symmetry
Dimension: 3D



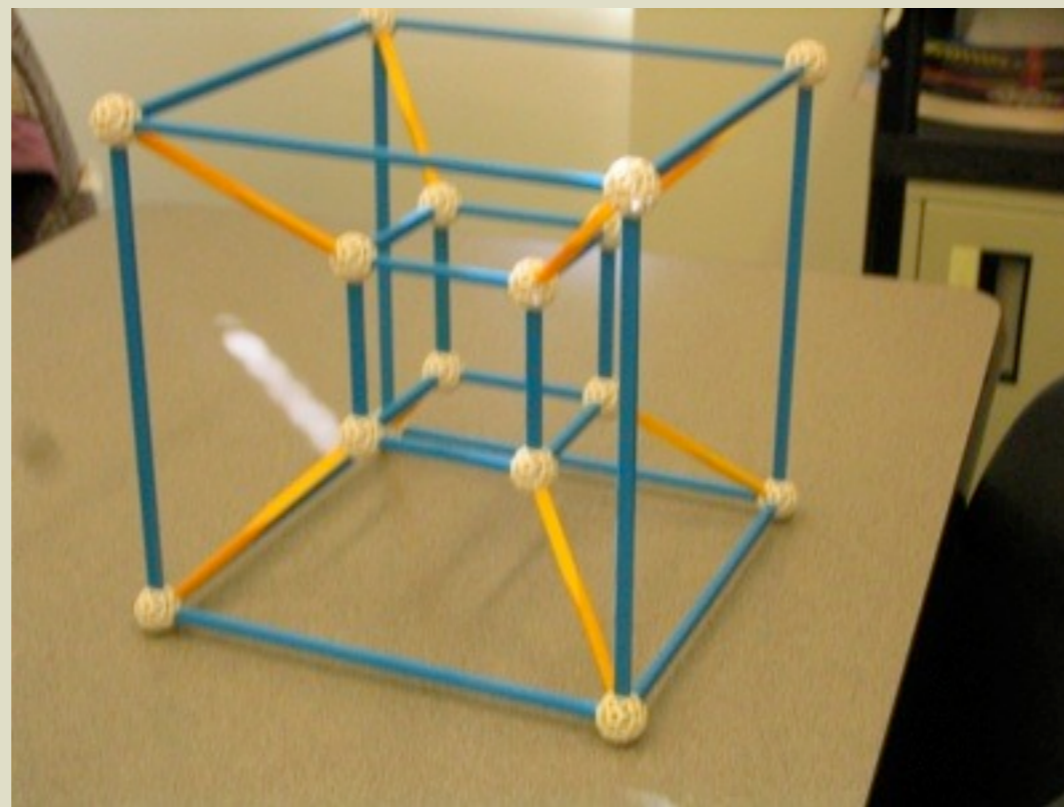
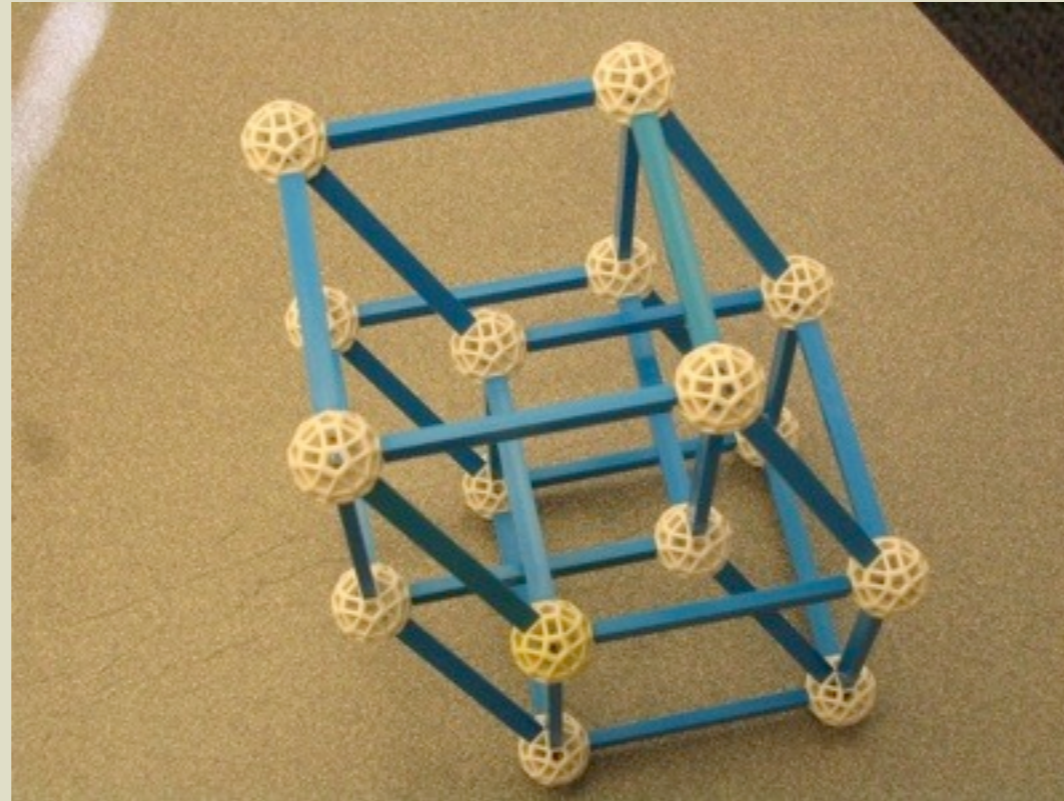
Transformations
Symmetry
Dimension: 3D



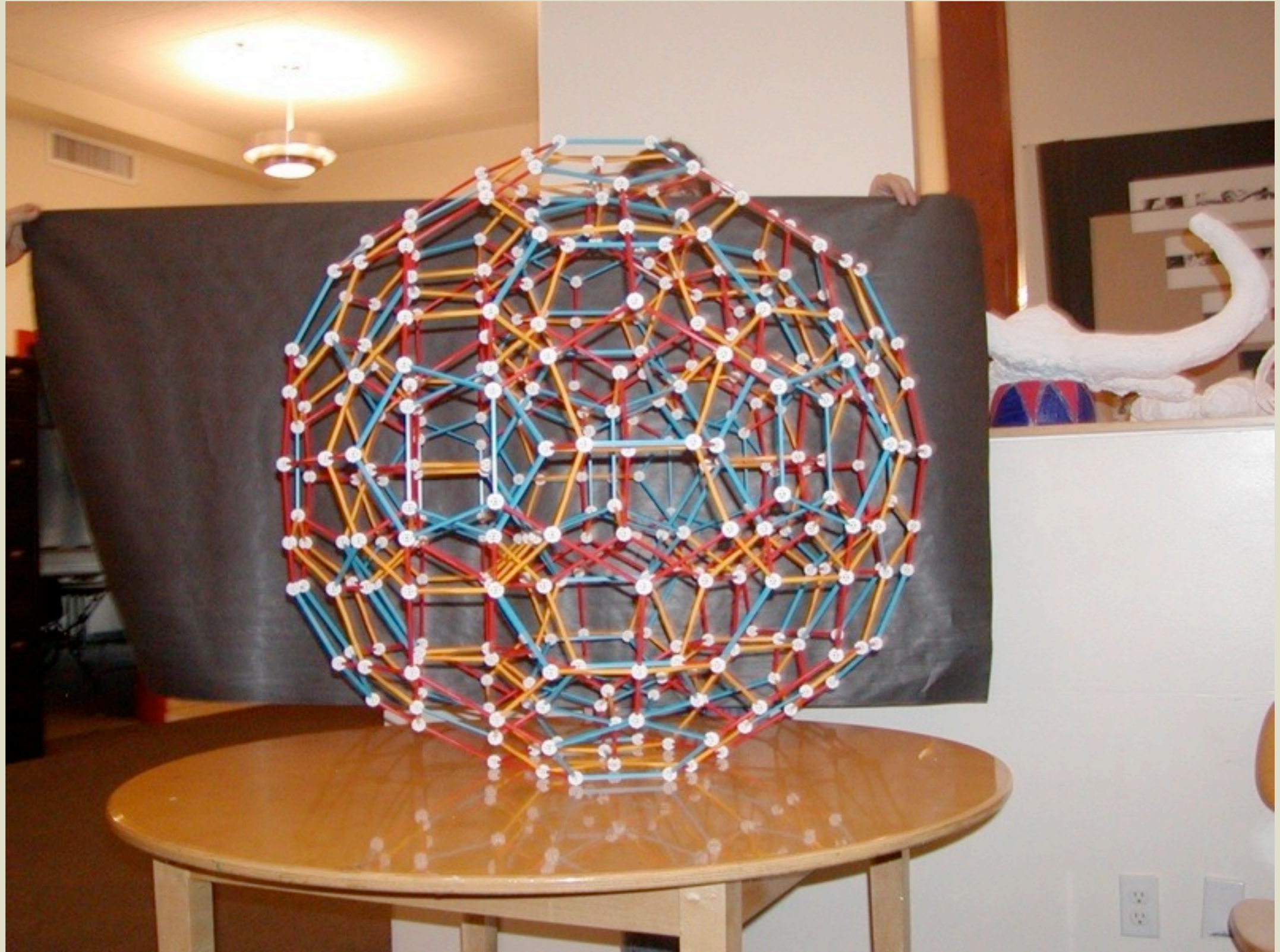
Transformations
Symmetry
Dimension: 4D



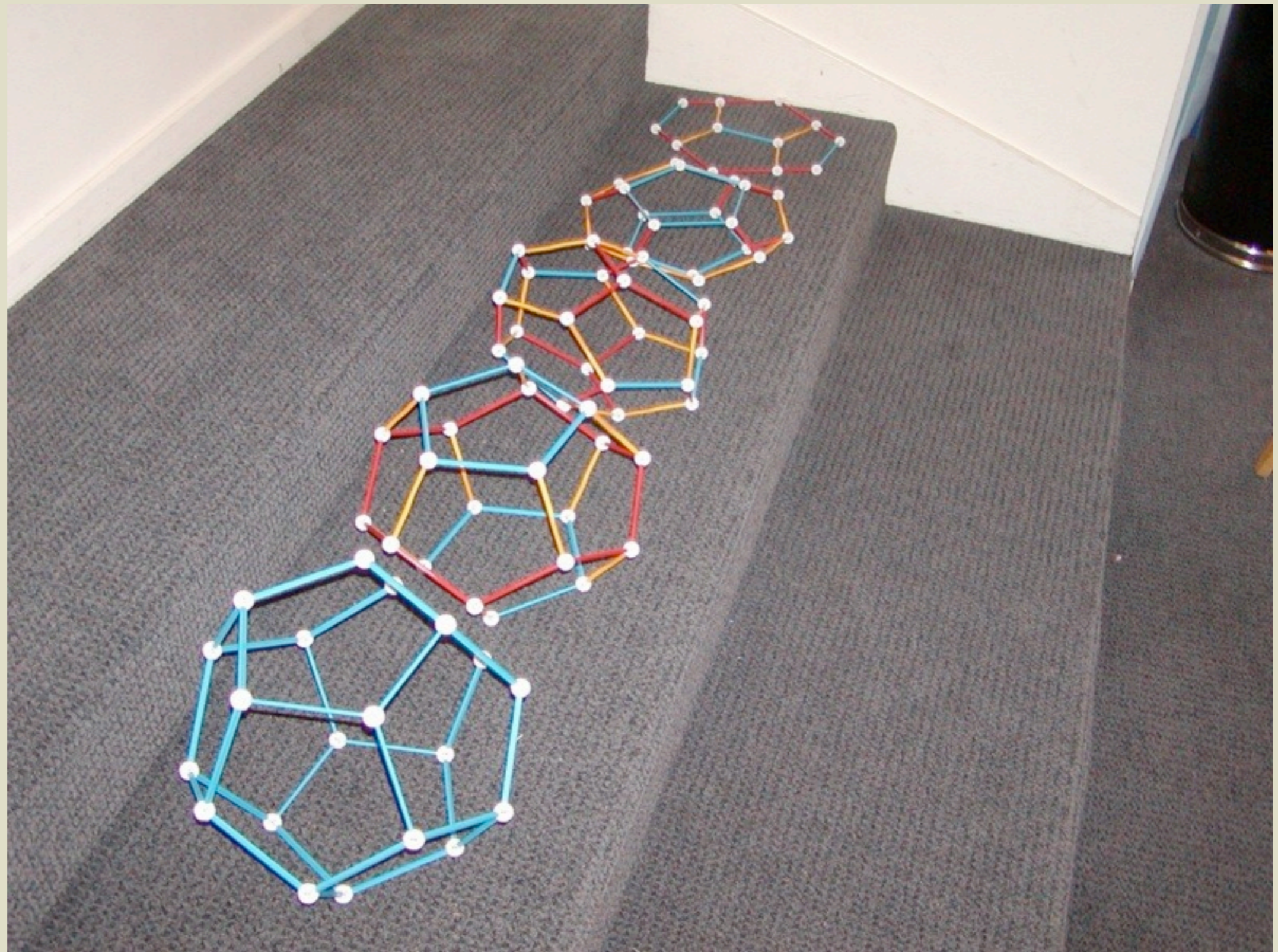
Transformations
Symmetry
Dimension: 4D



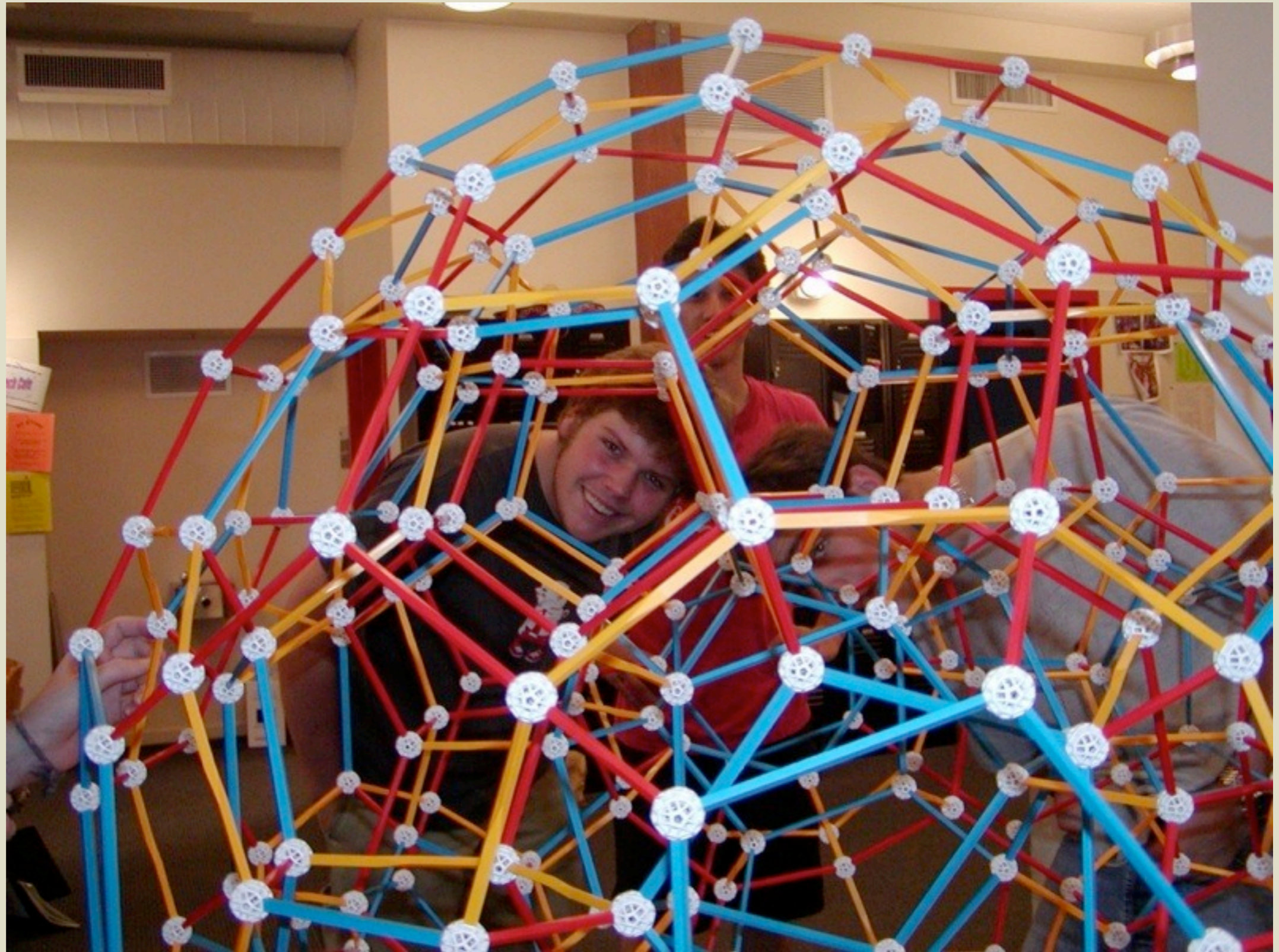
Transformations
Symmetry
Dimension: 4D



Transformations
Symmetry
Dimension: 4D



Transformations
Symmetry
Dimension: 4D



Space

An Alternate Elective after Algebra II

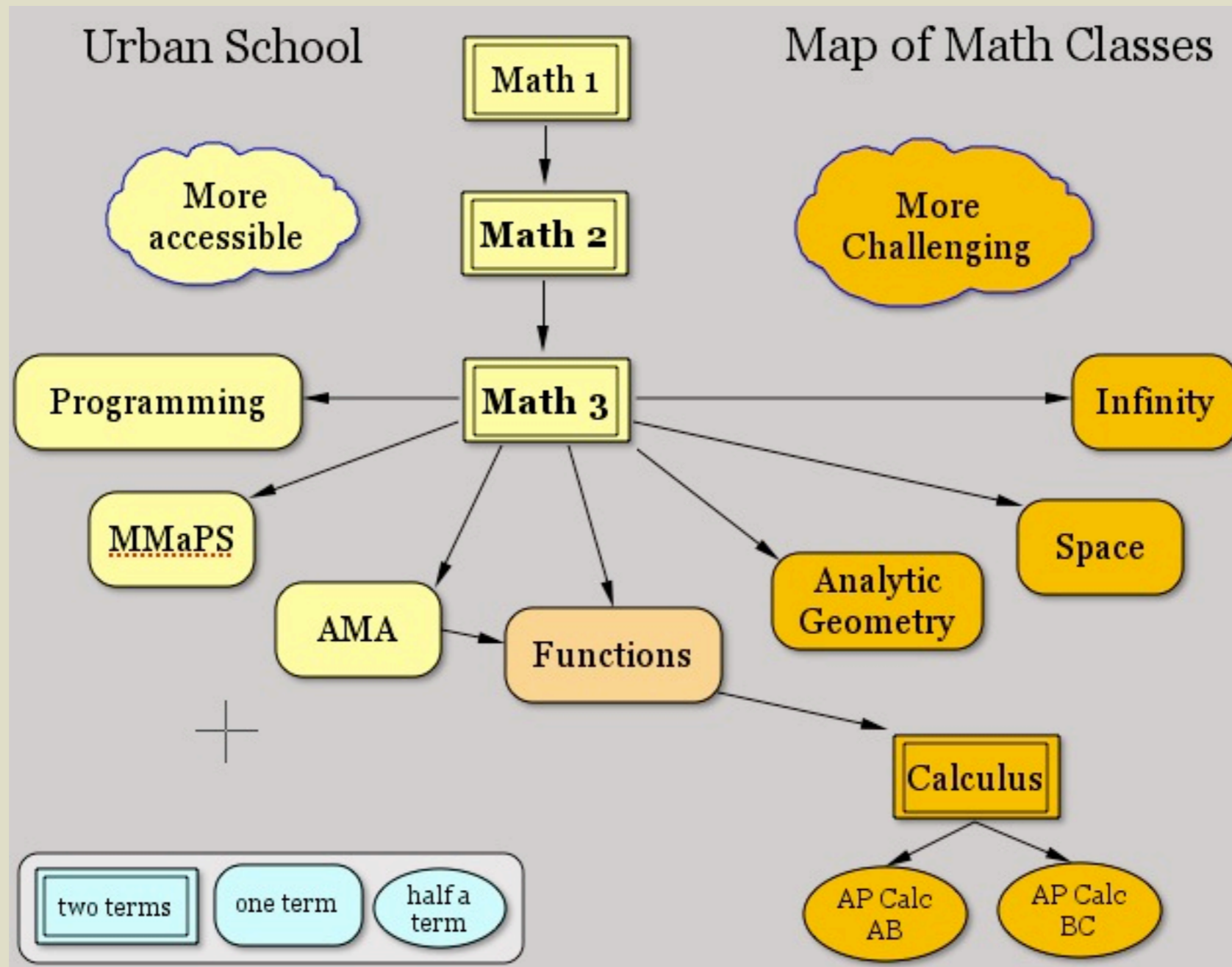


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Space overview

Who takes the class

Topics

Juniors, before
Calculus

Review

Seniors, instead of
or in addition to
Calculus

Resources

Electronic tools

Space overview

Who takes the class

Topics

Abstract algebra

Transformations

Review

Symmetry

Resources

Dimension (3D, 4D)

Electronic tools

Space overview

Who takes the class

Topics

Review

Resources

Electronic tools

Algebra

Geometry

Trigonometry

Space overview

Who takes the class

Transformational Geometry
by Richard Brown

Topics

Algebra: Themes, Tools, Concepts
by Anita Wah and Henri Picciotto

Review

Geometry Labs by Henri Picciotto

Resources

Handbook of Regular Patterns
by Peter Stevens

Electronic tools

Zome Geometry
by George Hart and Henri Picciotto

Flatland by Edwin Abbott

Space overview

Who takes the class

Topics

Cabri II+

TI-89

Review

Cabri 3D

Resources

Electronic tools

Space

An Alternate Elective after Algebra II



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