

## 12.A Equations from Data

Each of the tables below gives four  $(x, y)$  pairs for a function. Each function is one of the following types and has an equation of the corresponding form.

Type of Function	Form of Equation
direct variation	$y = mx$
inverse variation	$y = k/x$
linear	$y = mx + b$

For each table in problems 1 through 6,

- decide whether the function is direct variation, inverse variation, or linear;
- find the equation of the function.

1.	$x$	$y$	2.	$x$	$y$	3.	$x$	$y$
	0.05	5		0.05	0.002		0.9	0.6
	0.5	0.5		0.5	0.02		1.5	1.0
	5	0.05		5	0.2		2.7	1.8
	50	0.005		50	2		5.1	3.4

4.	$x$	$y$	5.	$x$	$y$	6.	$x$	$y$
	200	125		0.01	0.73		4	-2
	100	62.5		0.1	0.55		8	-1
	120	75		1.5	-2.25		18	1.5
	320	200		3	-5.25		25	3.25

7. Each of the following three tests can be used to recognize a certain type of function among direct variations, inverse variations, and linear functions. Match the test to the type of function. Make sure your answer works for problems 1-6.

- constant  $xy$  product
- constant slope
- constant  $y/x$  ratio

Because of measurement error, the numbers obtained in scientific experiments do not usually give perfect number patterns. For tables 8-10, find an equation that is approximately right.

8.	$x$	$y$	9.	$x$	$y$	10.	$x$	$y$
	1.5	0.50		12.5	6.8		0.6	4.12
	1.6	0.53		13	6.5		0.7	4.26
	1.7	0.55		13.5	6.3		0.8	4.37
	1.8	0.60		14	6.1		0.9	4.49
	1.9	0.63		14.5	5.9		1.0	4.61
	2.0	0.65		15	5.6		1.1	4.71

11. **Report** Summarize what you know about how to find the equation corresponding to experimental data, if it is one of the following types:

- direct variation
- linear function
- inverse variation

Include examples. Explain both how to recognize the type of function and how to find the actual equation.